Statistics with the TI-89

The TI-89 Manual, besides coming with your calculator, can be downloaded or read in a browser in Adobe Acrobat Reader form from <u>http://education.ti.com/product/pdf/gb/eng/8992p/\$8992book-eng.pdf</u>.

Using Graphlink to Transfer Variables, Files, and Flash Applications

You can link two TI-89's to transfer variables, files, and flash applications. To do this, you connect the calculators by the linking cable that comes with each calculator. Make sure that it is inserted securely in each calculator. How to do this is found in Chapter 22 of the Manual. You can also purchase a graphlink cable and software that allows transfer of data from the calculator to and from a computer and the internet.

Receiving Files. If you have the receiving calculator, hit 2nd [VAR-LINK] [F3](Link)->2:Receive to receive files, folders and/or flash applications and 2nd [VAR-LINK] [F3](Link)->5:Receive Product SW to receive operating system updates, which may be necessary to get new flash applications. You then get the WAITING TO RECEIVE and BUSY indicators on the status line. This means the calculator is ready to receive a transmission. To cancel this receive mode or to stop any transmission from either the receiving or sending unit, press ON followed by ESC in the error window that opens. Once transmission begins, messages requiring response may be received on the screen. If these are not self-explanatory, refer to the Manual.

Sending files. To transmit files to another calculator, hit 2nd [VAR-LINK]. You then select (and/or deselect) the variables or folders to send using the [F4]($\sqrt{}$) key. To transmit Flash Applications, first hit [F2](View) \odot 2:FlashApps [ENTER]. Once the items to transmit have been chosen and the receiving calculator is in receiving mode, hit [F3](Link)->1:Send to TI-89/92 Plus.

To transmit an updated operating system to the other calculator, hit 2nd [VAR-LINK] [F3](Link)->4:Send Product SW.

Installing the Inferential Statistics and Distribution Features

In all that follows, except possibly for random numbers, use the Stats/List Editor Flash Application. You will need to acquire this either from the internet using graphlink or from another TI-89 that has it using the linking method described above. A manual for the Stats/List Editor is on my web site and is available at http://education.ti.com/product/pdf/gb/statsle.pdf.

To use the Stats/List Editor application, hit <u>APPS</u>->1:FlashApps, then navigate to the Stats/List Editor using the direction arrows and hit <u>ENTER</u>. In the folder selection window that opens, unless you wish to create a new folder for your Statistics Applications, just hit <u>ENTER</u>. To switch back and forth between the Stats/List Editor application and the home page, just hit <u>2nd</u> [==]. Of course, pressing <u>HOME</u> also returns you to the home page at any time.

Working with Lists

Editing lists with the TI-89. When opening the Stats/List Editor, there are six lists that are usually opened by default, named list1through list6. Lists are saved to list variables. Any legal variable name

can be used. To enter a list called **protein**, whose elements are listed below, use the up arrow key to move the cursor to the top row, and then the right arrow key to move horizontally until you reach a blank column. See Figure 1. Then type **protein** and hit **ENTER**.

(F4_) F3_ (F3_) F4_) F5_ (F6_)	
Tools Algebra Calc Other Pr9mID Clean Up	
rand(10)	-6
rand(10)	5
rand(10)	8
rand(10)	1
$= \operatorname{seq}(\operatorname{nerd}(10) \times 1 \times 10) + u$	-
14 10 3 8 10 3 4	
seq(rand(10),x,1,10)→w	
MAIN RAD AUTO FUNC	
Figure 1	

F1+ F2+ ToolsPlots	F3+F4+F ListCalcDis	5+ F6+ F7+ itr Tests ints	
list5	list6	prote	
		35.9 41.98 44.4 44.73 47.23 51.16	
<u>proteir</u>	<u>n={35.9</u>	<u>,41.98,</u>	44.4,
MAIN	RAD AUTI	I FUNC	7/7
	Figur	e 2	

Now successively punch in each of the 61 elements in the list, each followed by \odot or ENTER.

35.90	41.98	44.40	44.73	47.23	51.16	51.70	53.07	54.07	54.38	54.41	55.05	55.47
57.68	57.73	57.90	58.50	59.20	59.36	59.76	61.10	61.70	61.90	62.20	62.32	62.80
63.96	66.60	67.10	67.20	69.91	70.17	71.50	72.10	72.20	72.30	73.50	73.53	74.78
76.33	77.40	77.63	78.15	79.55	82.60	83.82	84.70	85.40	86.24	88.17	88.78	91.47
95.06	95.33	100.36	106.00	109.30	114.79	128.40	149.49	153.56				

When editing an already entered list, use the arrow keys to move horizontally to the list you want to work with. Then edit the list, adding or changing items as necessary. You can delete any element of a list by hitting the - key when the cursor is on that element. To choose a different list to work with, use the arrow keys to move horizontally onto the list you want. If the list you want to work with is not displayed in the list editor, move to a blank spot in the top line, hit [F3](List)->1:Names, and, using the up and down arrow keys, scroll to the list you wish and then hit [ENTER]. Of course, you could also just type in the list name, as you do if creating a new list. In either case, now hit \odot or [ENTER]. You can remove a list and all its elements from the editor by hitting the - key when the cursor is on the list's name. To sort the list protein into ascending order, make sure the cursor is on the list's name and then hit [F3](List)->2:Ops->1:Sort List [ENTER]. The list should now be sorted in ascending order. See Figure 2.

Entering lists on the home page. Lists can be entered manually on the home page by beginning with a left brace "{" (hit 2nd (), typing in the numbers separated by commas, and ending with a right brace "}" (hit 2nd ()). Suppose you have two lists as follows:

X	10	8	13	9	11	14	6	4	12	7	5
у	7.46	6.77	12.74	7.11	7.81	8.84	6.08	5.39	8.15	6.42	5.73

Also, suppose you want to save the x list as listx and the y list as listy since these lists will be used later. Start with the x list. After hitting [CLEAR] to clear the entry line, type in the first list. To save the list as listx, hit the **STOP** key. Then hit 2nd alpha listx alpha [ENTER]. See Figure 3. (2nd alpha puts one in alpha lock and the last alpha releases that mode.)

F1+ F2+ F3+ F4+ F5 F6+	F1+ F2+ F3+ F4+ F5
ToolsA13ebraCa1cOtherPr3mlOClean Up	ToolsAl9ebraCalcOtherPr9mlOClean UP
	• (10 8 13 9 11 14) (10 8 13 9 11 14)
■ (10 8 13 9 11 14)	(7.46 6.77 12.74 7.1)
(10 8 13 9 11 14)	(7.46 6.77 12.74 7.1)
,11,14,6,4,12,7,5)→listx	39,8.15,6.42,5.73}→listy
Main g Rad auto Func 1/30	MAIN RAD AUTO FUNC 2730
Figure 3	Figure 4

The y list can similarly be entered as listy. See Figure 4.

Random Numbers on the TI-89

Random number commands native to the operating system of the TI-89 are:

[Ind [MATH]->7:Probability->4:rand(. The command rand() returns a random number > 0 and < 1 after ENTER is punched. Continuing to punch ENTER generates more random numbers. The command rand(20), for instance, will generate a random integer between 1 and 20. Similarly, rand(-20) will generate a random integer between -1 and -20.

[2nd [MATH]->7:Probability->5:randNorm(. The command randNorm(*MEAN*, *SD*) returns a random real number from a normal distribution specified by MEAN and SD.

[2nd [MATH]->7:Probability->6:randSeed. The command randSeed n where n is an integer resets the seed to the system default if n is 0 and generates two seeds saved to the system variable Seed1 and Seed2 if n is not 0.

You can find more about this on page 463 of the TI-89 Manual.

Random Numbers with the Stats/List Editor

From within the List Editor, the random number commands are found at [F4](Calc)->4:Probability. Typically, you would be interested in generating a list of random numbers. To do this, put the cursor on the name of an empty list and then put one of the following commands on the entry line:

[F4](Calc)->4:Probability->1:Rand83([*NUMTRIALS*]). NUMTRIALS random numbers > 0 and < 1 are generated. If NUMTRIALS is left blank, a single random number is generated.

[F4](Calc)->4:Probability->5:RandInt(LOW, UP, [NUMTRIALS]). Returns NUMTRIALS random integers bounded by the specified integers, $LOW \leq \text{integer} \leq UP$.

[F4](Calc)->4:Probability->6:.RandNorm([$\mu,\sigma,NUMTRIALS$]). Returns NUMTRIALS random real numbers from a normal distribution specified by mean μ and standard deviation σ .

[F4](Calc)->4:Probability->7:RandBin(N, P,[NUMTRIALS]). Returns NUMTRIALS random real numbers from a binomial distribution, where the number of trials $N \ge 1$ and $0 \le$ probability of success $P \le 1$.

[F4](Calc)->4:Probability->8:RandSamp(*LIST1*,*CHOOSE*[,*NOREP*=1]) Returns a *LIST* containing a random sample of the size you *CHOOSE* from *LIST1* with an option for sample replacement or no sample replacement (*NOREP*=1 or 0). The default is with sample replacement (1).

You can find more about these commands on pages 101-112 of the Stats/List Editor Manual.

Descriptive Statistics

One variable statistics with the TI-89. Suppose you wish to find the descriptive statistics for the list protein. Assuming the list is properly prepared and that you are in the List Editor, hit $[F4](Calc) \rightarrow 1:1$ -Var Stats. In the window that opens, with the cursor in the box for list, type the list name (protein here) or find it by hitting 2nd VAR-LINK and then using the arrow keys to navigate to the variable protein, where you will then hit ENTER to put it in the box (see Figure 5), hit ENTER again to accept it, and then hit ENTER one last time to get the statistics. See Figure 6. You can get any hidden results by hitting \bigcirc or \bigcirc . From top to bottom you have the mean, the sum of the data entries, the sum of the data entries squared, the sample standard deviation, the population standard deviation, the number of data points, the minimum value, the first quartile value, the mean. When you are finished viewing the statistics, hit ENTER].



Two variable statistics with the TI-89. This is similar to one variable statistics with the exception that two lists need to be entered in the provided boxes. Where data is paired, such as with listx and listy, a scatter plot of the data may be prepared. From the List Editor, hit [F2](Plots)->1:Plot Setup, and with the cursor on Plot1 (or any other plot you prefer), hit [F1](Define). If Scatter is not showing as Plot Type, hit ()1:Scatter. This is followed by \odot , where, unless the Mark you want is chosen, press, for instance, ()1:Box to choose boxes to mark the points. Hit \odot again, and in the box for x, either type in listx or choose it from the list under [2nd][VAR-LINK] as illustrated above under one variable statistics. Then hit \odot once more and, as above, enter listy for y. After another \odot , making sure Use Freq and Categories? is set to NO, press [ENTER]. See Figure 7. You now notice a $\sqrt{}$ in front of Plot1 and an abbreviated description of the plot following it. Defined plots may be selected and deselected by moving the cursor to the plot and choosing [F4]($\sqrt{}$ from the menu. With Plot1 selected, hit [F5](ZoomData) to get the scatter plot in a window selected to show all of the data points. See Figure 8. To return to the List Editor, hit [2nd] [IFE].



Regression with the TI-89. The Stats/List Editor on the TI-89 supports several types of regression, among which are linear, quadrfatic, cubic, quartic, logarithmic, exponential, power, and multiple linear. All of them work pretty much the same, so linear regression will be used as an example.

Use the lists listx (the x's) and listy (the y's) entered earlier. You have seen the scatter plot in the previous section. To find the linear regression equation, hit [F4](Calc)->3:Regressions-> 1:LinReg(a+bx). In the window that opens, as above, enter listx for X List and listy for Y List. Moving the cursor to the line Store RegEqn to: (See Figure 9), if you wish to graph the regression line, press (), then hit () until you get to the equation you want, such as y1(x), and press ENTER. Then press ENTER again to get the results. See Figure 10. The regression equation is y=3.00245+.499727x, the coefficient of determination $r^2=.666324$ and the correlation coefficient is r=.816287. When you are finished looking at the results, hit ENTER to return to the List Editor. There you will notice a new list named Resid, the residuals of the regression.



At this point, if you hit [F2](Plots)->1:Plot Setup and then make sure the cursor is on the appropriate plot, Plot1 in this example, and that the plot is selected pressing [F5](ZoomData), you now get the scatter plot with the regression line. See Figure 11.



We will next plot the residuals. Hit 2nd [\pm] to return to the List Editor. Use the instructions above under two variable statistics to define Plot2 (or any other plot number you choose) with the lists listx and vars\resid (the list resid found in the STATVARS folder – you may need to place the cursor on STATVARS and press () to open it. After hitting the final ENTER that returns you to the Plots screen, move the cursor to Plot1 and hit [F4]($\sqrt{}$) to deselect it. Then pressing [F5](ZoomData) gives you the residual plot. See Figure 12.

You can estimate and predict based on the regression equation. Suppose you wish to do this for x values of 9 and 15. Go to your home page by hitting HOME. Hit 2nd[VAR-LINK]. Navigate by arrows to y1. See Figure 13. Pressing ENTER places y1(on the entry line, which you should complete to y1(9). Then press ENTER to get the result of 7.5. See Figure 14. Since the last entry is still highlighted, press OC = 15 ENTER to get y1(15)=10.4984.



Probability Distribution Functions on the TI-89

Binomial Distribution. Assume that for a sample of n=15 you have that p = .75. You want to find first $P(X=6 \mid 15, .75)$. We can compute this probability by using the **binomial probability density function**

$$f(x) = \binom{n}{x} p^{x} (1-p)^{n-x}, x = 0...n.$$

After putting yourself in the List Editor, hit [F5](Distr)->B:Binomial Pdf. In the window that opens, enter 15 for Num trials, n, .75 for Prob Success, p, and 6 for X Value. See Figure 15.



Then hit $\overline{\text{ENTER}}$ to get the results screen in Figure 16. You see that P(X=6 | 15, .75)=.003398. If Value is left blank, the result screen shows a list of Pdf values, and hitting ENTER adds the list Pdf to the List Editor where the values for x=0 through x=15 can be found. Keep in mind, however, that in the entry line Pdf[n] corresponds to x=n-1. See Figure 17.

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To find $P(X \le 5 \mid 15, .75)$, use the **binomial cumulative density function**. Similar to what you did above hit [F5](Distr)->C:Binomial Cdf. In the window that opens, enter 15 for Num trials, n, .75 for Prob Success, p, 0 for Lower Value, and 5 for Upper Value. See Figure 18. Then hit ENTER to get the results screen in Figure 19. You see that $P(X \le 5| 15, .75) = .000795$. Leaving both Lower Value and Upper Value blank results in a list Cdf similar to the list Pdf above. See Figure 20.



To find $P(6 \le X \le 9 \mid 15, .75)$, just use 6 for Lower Value and 9 for Upper Value.

Poisson Distribution. Assume that $\lambda = .5$. You want to find P(X=1 | .5), P(X \le 7 | 2.2), and P(4 \le X \le 9 | 2.2). You can compute these probabilities by using the **Poisson probability density function**

$$f(x) = \frac{e^{-\lambda}\lambda^x}{x!}, x = 0, 1, 2, \dots$$

or the **Poisson cumulative density function**. These are implemented similar to the binomial probability and cumulative density functions above by the commands [F5](Distr)–>D:Poisson Pdf and [F5](Distr)–>E:Poisson Cdf with the difference that there is now a box for λ and the various value boxes cannot be left blank. You will find that P(X=1 | .5)=.303265, P(X \le 7 | 2.2)=.998022, and P(4 \le X \le 9 | 2.2)=.180547.

Normal Distribution. The normal probability density function is given by

$$f(x) = \frac{1}{\sqrt{2\pi\sigma}} e^{\frac{-(x-\mu)^2}{2\sigma^2}}, \sigma > 0.$$

Assume $\mu = 100$ and $\sigma = 20$. To find f(110), for instance, hit [F5](Distr)->3:Normal Pdf. In the window that opens, put in 110 for X Value, 100 for μ , and 20 for σ . Hitting ENTER then gives you the results screen in Figure 21, where you see that f(110)=.017603. Suppose you wish to plot the normal curve for these parameters. Go back to your home screen and hit \bigcirc [WINDOW], and set the window parameters, to xmin=40, xmax=160, xscl=20, ymin=0, ymax=.05, yScl=1, and xRes=1. This will





Figure 22

allow you to see the curve a distance of three standard deviations from the mean in both directions and cause tick marks to be placed along the x-axis at intervals of one standard deviation. Now hit \bigcirc [Y=] and by using \bigcirc , \bigcirc , and [F4](\checkmark) as necessary, deselect all plots and functions other than y1, and move the cursor onto y1. Then hit [CLEAR] [CATALOG][F3](flash Apps), and then use the arrow keys to navigate to normPdf(. At the bottom of the screen, you will now see X[, μ , σ]. This indicates that three parameters are needed to complete the function, X, μ , and σ , just as were entered in the box above. The brackets are around μ and σ to indicate that they are optional, the defaults being the 0 nd 1 of the standard normal distribution. Now hit [ENTER] and complete the command to TIStat.normPdf(x,100,20). See Figure 22. Then hit \bigcirc [GRAPH] to see the curve. See Figure 23.



To find P(X \leq 115) using the same distribution, you need the **normal cumulative distribution function**. Go to the List Editor and hit [F5](Distr)–>4:Normal Cdf. In the window that opens, leave Lower Value blank. This then uses the default of $-\infty$ for Lower Value. Enter 115 for Upper Value (leaving this box blank is the same as ∞), 100 for μ , and 20 for σ . See Figure 24. Then hit ENTER to get the results screen in Figure 25. You get that P(X \leq 115) = .773373. Again, not including the mean and standard deviation will result in the assumption of the standard normal distribution. To find P(X \geq 95), you would use 95 for Lower Value and leave Upper Value blank. To find P(90 \leq X \leq 135), you would use 90 for Lower Value and 135 for Upper Value.



To find x_1 such that $P(X \le x_1) = .975$, which is useful for finding critical values for hypotheses tests, go first to the List Editor. You will use the **inverse normal distribution function**. This is the inverse of the normal cumulative distribution function. Hit [F5](Distr)->2:Inverse->1:Inverse Normal. In the screen that opens, enter .975 for Area, 100 for μ , and 20 for σ . See Figure 26. Then press ENTER to get the screen in Figure 27. You see that $x_1=139.199$.







Student's *t* **Distribution.** The **cumulative** *t* **distribution** can be used to compute probabilities such as $P(t \ge 1.23 | df = 18)$ or P(t < -1.42 | df = 9). This procedure is similar to that of the normal cumulative distribution function, except that there is a box for degrees of freedom and none for mean and standard deviation. To find the former, hit [F5](Distr)->6:t Cdf and complete the screen that appears as in Figure 28. After hitting [ENTER], you find from the results screen that $P(t \ge 1.23 | df = 18) = .117266$. The *t* **probability distribution function** is applied similar to that of the normal probability distribution function beginning with [F5](Distr)->5:t Pdf.

To find t_1 such that $P(t \ge t_1 | df=15) = .025$, which is useful for finding critical values for hypotheses tests, go first to the List Editor. You will use the **inverse** *t* **distribution function**. This is the inverse of the *t* cumulative distribution function. Hit [F5](Distr)->2:Inverse->2:Inverse t. In the screen that opens, enter .025 for Area and 15 for Deg of Freedom, df. See Figure 29. Then press ENTER to get the screen in Figure 30. You see that $t_1=-2.13145$.



 χ^2 Distribution. The cumulative χ^2 distribution can be used to compute probabilities such as P($\chi^2 \ge 24$ ldf=16). This procedure is similar to that of the normal cumulative distribution function, except that there is a box for degrees of freedom and none for mean and standard deviation. To find this value, hit [F5](Distr)->8:Chi-square Cdf and complete the screen that appears as in Figure 31. After hitting [ENTER], you find from the results screen that P($\chi^2 \ge 24$ ldf=16) = .089504. The χ^2 probability distribution function is applied similar to that of the normal probability distribution function beginning with [F5](Distr)->7:Chi-square Pdf.



Figure 31



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To find $(\chi^2)_1$ such that $P(\chi^2 \ge (\chi^2)_1 | df=28) = .95$, which is useful for finding critical values for hypotheses tests, go first to the List Editor. You will use the **inverse** χ^2 **distribution function**. This is the inverse of the χ^2 cumulative distribution function. Hit [F5](Distr)->2:Inverse->3:Inverse Chi-square. In the screen that opens, enter .95 for Area and 28 for Deg of Freedom, df. Then press <u>ENTER</u>. You see that $(\chi^2)_1=41.3371$.

F Distribution. The cumulative **F** distribution can be used to compute probabilities such as P(F \geq 20lnum df=3,den df=6). This procedure is similar to that of the normal cumulative distribution function, except that there are two boxes for degrees of freedom and none for mean and standard deviation. To find this value, hit [F5](Distr)->A:F Cdf and complete the screen that appears as in Figure 32. After hitting [ENTER], you find from the results screen that P(F \geq 20lnum df=3,den df=6)= .001586. The **F** probability distribution function is applied similar to that of the normal probability distribution function beginning with [F5](Distr)->9:t Fdf.

To find F_1 such that $P(F \ge F_1 | \text{num df} = 5, \text{den df} = 8) = .99$, which is useful for finding critical values for hypotheses tests, go first to the List Editor. You will use the **inverse F distribution function**. This is the inverse of the F cumulative distribution function. Hit [F5](Distr)->2:Inverse->4:Inverse F. In the screen that opens, enter .99 for Area, 5 for Num df, and 8 for Den df. Then press ENTER. You see that $F_1=63183$.

Inferential Statistics on the TI-89

Begin by entering two lists of data from two independent samples. As an example, cadmium level determinations were made on the placentas of two groups of mothers in nanograms per gram. The first group of 18 mothers were nonsmokers (ns), while the second group of 14 mothers were smokers (sm).

ns: 10.0 8.4 12.8 25.0 11.8 9.8 12.5 15.4 23.5 9.4 25.1 19.5 25.5 9.8 7.5 11.8 12.2 15.0 sm: 30.0 30.1 15.0 24.1 30.5 17.8 16.8 14.8 13.4 28.5 17.5 14.4 12.5 20.4

ns has a mean of 14.72 and a standard deviation of 6.20, while sm has a mean of 20.41 and a standard deviation 6.81.

Confidence Interval for a Population Mean. To find a 95% confidence interval for the mean of ns, make sure you are in the List Editor and hit [2nd][F7](Ints)->2:TInterval. In the first screen that comes up, choose Data, hit [ENTER], and then fill in the second screen as in Figure 33. Then hit [ENTER]. You are given (11.64,17.8) as the confidence interval, along with the point estimate (x-bar=14.7222), margin of error (ME=3.08251), degrees of freedom (df=17), sample standard deviation (Sx=6.19863), and sample size (n=18). See Figure 34.



Figure 33

Figure 34

If a data list isn't in the calculator, but you know the standard deviation and mean, when you get to the choice of Data vs. Stats, choose Stats, hit ENTER, and then fill in the boxes as shown in Figure 35. Here you also get the same confidence interval of (11.64,17.8), although some of the other statistics are just a bit different from above since more rounding was done here for the mean and standard deviation.







If the population standard deviation σ is known, you can make use of the normal distribution by choosing 2nd [F7](Ints)->1:ZInterval instead of 2nd [F7](Ints)->2:TInterval.

Confidence Interval for the Difference Between Two Population Means. Use ns and sm as data. To find a 95% confidence interval for the difference of the means of ns and sm, hit 2nd [F7](Ints)->4:2-SampTInt. In the first window that comes up, choose Data. Again, do this since the data has been entered as lists. Now hit ENTER and fill in the boxes of the second window with ns for List1, sm for

List2, 1 for both Freq1 and Freq2, and .95 for C Level. For Pooled (pooled variance), assuming that it is not known that the population variances are equal, choose NO (YES for equal variances). See Figure 37. Then hit ENTER to get the results. As you can see from Figure 38, you are given a confidence interval of (-10.5, -.899) along with other relevant results.

If the population standard deviations are known, you can use <u>2nd[F7](Ints)->4:3-SampZInt</u> instead of <u>2nd[F7](Ints)->4:2-SampTInt</u>, making use of the normal distribution.



Confidence Interval for a Population Proportion. You want a 99% confidence interval for the proportion of a certain population of boys who have attempted suicide. Of a sample of 96 boys, 18 had attempted suicide. Hit [2nd][F7](Ints)–>5:1-PropZInt. For Successes, x, enter 18; for n, enter 96; and for C Level, enter .99. Then hit [ENTER]. You are given an interval of (.0849,.29013) with a p-hat of .1875.

Confidence Interval for the Difference between Two Population Proportions. 60 of 123 girls from a related population have attempted suicide. Hit [2nd][F7](Ints)->6:2-PropZInt. For Successes, x1, enter 18; for n1, enter 96; for Successes, x2, enter 60; for n2, enter 123; and for C Level, enter .99. Then hit [ENTER]. You are given an interval of (-.455,-.1453) with a p-hat1 of .1875 and a p-hat2 of .487805.

Confidence Interval for Linear Regression using *t***.** Return to the earlier linear regression example using listx and listy. Hit 2nd[F7](Ints)–>7:1-LinRegTInt. One of the choices in the page that opens is Response or Slope.

In the **Response** case, an X Value is required to determine a calculated y value, y_hat, at which point a prediction confidence interval around y_hat is determined, as well as a confidence interval for the mean. Complete the window as in Figures 39 and 40, noticing the use of an X Value of 10. Notice also the arrows on the left side of the window indicating some values are off screen, necessitating scrolling.



Then hit <u>ENTER</u>. The results screen is shown in Figures 41 and 42, scrolling again being necessary to see it all. In Figure 41, the 99% confidence interval C Int=(6.729,9.27) is for the mean of y_hat(10), and in Figure 42 the 99% confidence interval pred Int=(3.786,12.213) is for y_hat(10). You can also

observe the regression data in Figure 42.



In the Slope case, LinRegTInt computes a linear regression T confidence interval for the slope coefficient b. If the confidence interval contains 0 this is insufficient evidence to indicate that the data exhibits a linear relationship. Entering the data as above, except for X Value, which is inaccessible, you get a 99% confidence interval C Int=(.1166,.88283) for the slope b. Since 0 is not in the interval, you can conclude the existence of a linear relationship. Again, the regression data is available.

Confidence Interval for Multiple Regression. Enter the following lists: listx1, listx2 and listy1 as given below.

listx1:	1	2	3	3.5	4.5
listx2:	4	3	2	1	1
listy1:	4	5	6	7	8

We are assuming that y1 is a function of x1 and x2. Hit $2nd[F7](Ints) \rightarrow 8:1$ -MultRegInt. This corresponds to the Response option above. In the first window that opens, choose 2 for Num of Ind vars and then hit ENTER. In the second window, fill in the boxes as shown in Figure 43. The X Value List of {2,3} corresponds to the point (x1,x2)=(2,3). Then press ENTER. The results screen is shown in Figures 44 and 45. In Figure 44, the 95% confidence interval C Int=(3.928,6.189) is for the mean of y_hat(2,3), and in Figure 45 the 99% confidence interval pred Int=(2.687,7.433) is for y_hat(2,3). You can also observe the regression data in both figures, with the regression equation, using B List. To find the values of Blist, after hitting ENTER, move the cursor onto a blank list name, hit 2nd[VAR-LINK], and scroll down to blist under STATVARS and hit ENTER]. From blist in the List Editor (see Figure 46), you can determine that the regression equation is y1=3.5882 + x1 - .1765 x2.







Hypothesis Testing for a Single Population Mean. Use as a null hypothesis H_0 : $\mu = 14$ for the data set ns and use a t-test. Hit 2nd [F6](Tests)->2:T-Test. In the first window that comes up, choose Data. Put 14 for μ 0, ns for List, 1 for Freq, and choose $\mu \neq \mu$ 0 for Alternate Hyp. For Results, choose Calculate. See Figure 47. Then hit ENTER. The results window gives t=.494324 and p=.627404 along with other results. See Figure 48.





Figure 48

To get a graphical representation instead, choose **Draw** instead of **Calculate** for **Results**. The t and p values are given below the graph with the p equaling the shaded area. See Figure 49. Notice that you are now in the graph page.



If the population standard deviation σ is known, you can make use of the normal distribution by choosing 2nd [F6](Tests)->1:Z-Test instead of 2nd [F6](Tests)->2:T-Test.

Hypothesis Testing for the Difference between Two Population Means. Use as a null hypothesis H_0 : $\mu 1 = \mu 2$ for the data sets ns and sm and use a t-test. Hit 2nd[F6](Tests)->4:2-SampTTest. Again, choose Data in the first window that opens and then press [ENTER]. Put ns for List1, sm for List2, 1 for Freq1 and Freq2, $\mu 1 < \mu 2$ for Alternate Hyp., No for Pooled, and Calculate for Results. See Figure 50. Notice that you have to scroll to get to all of the options. Then hit [ENTER]. The results window gives t=-2.43759 and p=.010862, along with other results. See Figure 51.

To get a graphical representation instead, choose **Draw** instead of **Calculate** for **Results**. The t and p values are given below the graph with the p equaling the shaded area. Again, notice that you are now in the graph page.

If the population standard deviations $\sigma 1$ and $\sigma 2$ are known, you can make use of the normal distribution by choosing 2nd[F6](Tests)->3: 2-SampZTest instead of 2nd[F6](Tests)-> 4:2-SampTTest.

F1: Too 2-Sample T Test	Too 2-Sample F Test
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
Nam (Enter=OK) MAIN RAD AUTO FUNC 13/12	Nan Enter=OK
Figure 51	Figure 52

Hypothesis Testing for comparing Two Standard Deviations. Use as a null hypothesis H_0 : $\sigma 1 = \sigma 2$ for the data sets ns and sm and use an F-test. We will also use as an alternate hypothesis H_A : $\sigma 1 < \sigma 2$. Hit 2nd[F6](Tests)–>9: 2-SampFTest. See Figure 42. Choose Data in the first window that opens and then press ENTER, filling in the rest of the boxes as in previous example (Figure 50). Then hit ENTER. The results window gives F=.82751 and p=.351256, along with other results. See Figure 52.

To get a graphical representation instead, choose Draw instead of Calculate for Results. The F and p values are given below the graph with the p equaling the shaded area. Recall that you are now in the graph page.

Hypothesis Testing for a Single Population Proportion. In a survey of injection drug users in a large city, 18 out of 423, i.e. p-hat = .0426, were HIV positive. Can one conclude that fewer than 5% of the population of injection drug users in the city are HIV positive. Use H_0 : p = .05, so H_A : p < .05. Hit 2nd [F6](Tests)->5: 1-PropZTest. Put in .05 for p0, 18 for Successes, x, 423 for n, Prop<p0 for Alternate Hyp., and Calculate for Results. Then hit ENTER. The results window gives z=-.702738 and p=.241109, along with other results. See Figure 53.



To get a graphical representation instead, choose Draw instead of Calculate for Results. The z and p values are given below the graph with the p equaling the shaded area. Recall that you are now in the graph page.

Hypothesis Testing for the Difference between Two Population Proportions. Return to the situation where 18 of 96 boys and 60 of 123 girls attempted suicide. Use as a null hypothesis H_0 : p1 = p2 with H_A : p1 < p2. Hit [2nd][F6](Tests)=>5: 2-PropZTest. For Successes,x1, enter 18; for n1, enter 96; for Successes,x2, enter 60; for n2, enter 123; and for Alternate Hyp., p1<p2. Then hit [ENTER]. The results window gives z=-4.60485 and p=.000002, along with other results. See Figure 54.

One-Way Anova. Enter three lists in the calculator, $a1=\{7, 4, 6, 6, 5\}$, $a2=\{6,5,5,8,7\}$, and $a3=\{4,7,6,7,6\}$. The null hypothesis here is $H_0: \mu 1=\mu 2=\mu 3$ with H_A : not all of $\mu 1, \mu 2, \mu 3$ are equal. To run the test, hit 2nd[F6](Tests)->C: ANOVA. In the first window that opens, choose Data and 3 for Number of Groups, and then hit ENTER. Complete the second window as in Figure 55. Then hit

ENTER. The results window gives F=.311111 and p=.738367, along with other results, some of which you have to scroll to see. See Figure 56.



Three new lists appear in the List Editor, as seen in Figure 57. The three lists are **xbarlist** (the means of the three lists) and **lowlist** and **uplist**, the left and right endpoints of the 95% confidence interval for each mean. For instance, the mean of list **a1** is 5.6 and the 95% confidence interval for that mean is (4.4066,6.7934).



Figure 57



We see the means x-bar of the three lists are 5.6, 6.2, and 6. We can find that the standard deviations Sx are 1.14018, 1.30384, and 1.22474, and each list has a sample size of 5. If you had chosen the **Stats** option instead of **Data**, for each group you enter a list $\{n,xbar,sx\}$ as prompted on the screen. See Figure 58. Then press ENTER to get the same results as before.

Two-Way Anova. Enter four lists in the calculator, a21={7, 4, 6, 6, 5,6}, a22={6,5,5,8,7,7}, a23={4,7,6,7,6,6}, and a24={4,7,8,9,5,7}. ANOVA2-Way computes a two-way analysis of variance for comparing the means of two to twenty populations (levels of factor A called LvIs of Col Factor). In the 2 Factor, Equal Repetitions design, each of the considered populations has an equal number of levels of factor B (LvIs of Row Factor). In the Block design, the levels of factor B are equal to the block. The ANOVA2-Way procedure compares the means of the experimental factors, factor A, factor B, and factor AB (the interaction effect). For each of the experimental factors, the null hypothesis H_0 : $\mu 1 = \mu 2 = ... = \mu k$ is tested against the alternative hypothesis H_A : not all of $\mu 1, \mu 2, ..., \mu k$ are equal. In the case of the Block design, there is no interaction effect.

Consider the Block design first. To run the test, hit 2nd[F6](Tests)->D: ANOVA2-WAY. In the first window that opens, choose Block for Design and 4 for LvIs of Col Factor, and then hit ENTER. Complete the second window as in Figure 59. Then hit ENTER. The results window gives first, under Factor, an F=.704225 and p=.56416 for the treatment (column) factor. See Figure 60. Scrolling down, in Figure 61 you see the F=1.56338 and p=.229969 for the Block factor. You can also see that further scrolling will provide the Error results.



Now to the 2 Factor, Equal Repetitions design. Hit $2nd[F6](Tests) \rightarrow D$: ANOVA2-WAY. In the first window that opens, choose 2 Factor, Eq Reps for Design, 4 for LvIs of Col Factor, 2 for LvIs of Row Factor, and then hit ENTER. Complete the second window as in Figure 59 above. Then hit ENTER. The results window gives first, under Column Factor, an F=.620155 and p=.612083. See Figure 62. Scrolling down, under Row Factor, you get F=2.32558 and p=.146785, and under Interaction, you get F=.589147 and p=.630932. You can also see that further scrolling will provide the Error results.

Chi-Square Goodness of Fit. Chi2 GOF performs the chi square goodness of fit test to confirm that sample data is from a population that conforms to a specified distribution. For example, **Chi2 GOF** can confirm that the sample data came from a normal distribution. Enter two lists in the calculator, $ch1=\{16,25,22,8,10\}$ (the observed values) and $ch2=\{9,12,9,8,7\}$ (the expected values if the data were from a particular distribution. To run the test, hit 2nd[F6](Tests)->7: Chi2 GOF. In the window that opens, choose ch1 for Observed List, ch2 for Expected List, Calculate for Results, and then hit



Figure 63

Figure 64

ENTER. The results window gives $\chi^2 = 39.5913$ and p=1.30073E-8=.000000013. See Figure 63. You will also find a new list in the List Editor, complist, which gives the element by element contributions to χ^2 , the sum of the items in the list. See Figure 64.

To get a graphical representation instead, choose Draw instead of Calculate for Results. The χ^2 and p values are given below the graph with the p equaling the shaded area.

Chi-Square Test of Independence. First enter a matrix of observed values. Call this matrix ob. Here [23 4 10]

use $ob = \begin{vmatrix} 23 & 4 & 10 \\ 10 & 14 & 35 \end{vmatrix}$. To enter the matrix, return to the home page (HOME) and hit

[APPS]->6:Data/Matrix Editor->3:New. Choose Matrix for Type, main for folder, type in ob for Variable, 2 for Rows, 3 for Columns, and then hit ENTER. See Figure 65. Then continue by hitting each number in succession followed by ENTER. See Figure 66. When you are finished, hit [HOME]. Then return to the List Editor.



To run the test, hit 2nd[F6](Tests)->8: Chi2 2-way. In the window that opens, enter ob for Observed Mat, statvars\expmat (the default) for Store Expected to, statvars\compmat (the default) for Store CompMat to, Calculate for Results (see Figure 67), and then hit ENTER.



Figure 67

Figure 68

The null hypothesis is that there is no association between the row and column variable, with the alternative hypothesis being that the variables are related. From Figure 68, you get a χ^2 of 20.6062 and a p-value of .000034.

To see the expected matrix, from the home page hit $\boxed{\text{APPS}}$ ->6:Data/Matrix Editor->2:Open. In the window that opens, choose Matrix for Type, statvars for folder, expmat for Variable, and hit $\boxed{\text{ENTER}}$. The matrix is in Figure 69. You can do the same to get compmat, the matrix of component contributions whose sum is χ^2 . See Figure 70.

To get a graphical representation instead, choose Draw instead of Calculate for Results. The χ^2 and p values are given below the graph with the p equaling the shaded area

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MAT							
223	c1	c2	сЗ				
1	12.719	6.9375	17.344				
2	20.281	11.063	27.656				
3							
4							
r1c1=12.71875							
MAIN	RAD	AUTO	FUNC				

F1+ Tools P	F2 1ot Setup C	3 611 (0. 50 er)	F64 F7 Cox Util Sta	e)			
MAT							
233	c1	c2	сЗ				
1	8.3109	1.2438	3.1095				
2	5.2119	.78001	1.95				
3							
4							
r1c1=8.3108875921376							
MAIN	RAD	AUTO	FUNC				

Figure 69

Figure 70

Hypothesis Testing for the slope and correlation coefficient in Linear Regression using *t***.** Return to the earlier linear regression example using listx and listy. LinRegTTest (linear regression *t* test) computes a linear regression on the given data and a *t* test on the value of slope **b** and the correlation coefficient **r** for the equation y=a+bx. It tests the null hypothesis H_0 : b=0 (equivalently, r=0) against one of the following alternatives: H_A : b≠0 and r≠0, H_A : b<0 and r<0, or H_A : b>0 and r>0. The first option will be used here. To run the test, from within the List Editor hit [2nd][F6](Tests)–>A: LinRegTTest. Fill in the window that opens as in Figure 71. Then hit [ENTER] to get the results window. See Figure 72. You see that you get t=4.23937 and p=.002176. Thus you can conclude that there is a linear relationship between the variables. You can see that the regression equation is y=3.00245+.499727x with a standard error of the estimate s=1.23631, and by scrolling down, that the coefficient of determination $r^2=.666324$ and the correlation coefficient is r=.816287. Resid, the list of residuals of the regression, is also added to the List Editor.



Hypothesis Testing for Multiple Regression. Return to the earlier multiple regression example using listx1, listx2, and listy1. MultRegTests computes a multiple regression on the given data yielding an equation Y=B0+B1*X1+B2*X2, an F test on the hypotheses H_0 : B1=B2=0 with H_A : not both B1, B2 equal to 0, *t* tests on the coefficients B1, B2, B3, and the coefficient of determination. To run the test, from within the List Editor hit [2nd][F6](Tests)->B: MultRegTests. Fill in the window that opens as in Figure 73. Then hit [ENTER] to get the results window. See Figure 74. You see that you get F=112.333 and p=.008824. Thus you can conclude that there is a linear relationship between the variables. You can see that the coefficient of multiple determination R^2 =.991176 and the standard error of the estimate is S=.210042. Several columns have been added to the List Editor. From the column blist we get the coefficients for the regression, yielding the equation Y=3.5882+1.000*X1-.1765*X2. Two columns to the right of blist is tlist, giving the t values for the corresponding B's, and one column to the right of that is plist, giving the corresponding p-values.



